

(Please write your Exam Roll No.)

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END TERM EXAMINATION

THIRD SEMESTER [MCA] DECEMBER-2012

Paper Code: MCA 201

Subject: Theory of Computation

Time : 3 Hours

Maximum Marks : 60

Note: Attempt five questions including Q. no. 1 which is compulsory. Select one question from each unit.

Q1 Answer the following :-

(2*10=20)

- (a) Give regular expression for the following :-
 - (i) $\{1^{2n+1}:n>0\}$ and (ii) $\{a^n:n \text{ is divisible by } 2 \text{ or } 3 \text{ or } n=5\}$.
- (b) Define multitape Turing Machine.
- (c) State Myhill-Nerode theorem.
- (d) Define derivation tree for CFG.
- (e) When a problem is said to be undecidable? Give an example of an undecidable problem.
- (f) State Post Correspondence Problem.
- (g) Show that $id+id*id$ can be generated by two distinct leftmost derivation in the grammar $E \rightarrow E+E \mid E*E \mid (E)id \mid$.
- (h) Convert the grammar $S \rightarrow aSb \mid ab$ into Chomsky normal form.
- (i) State Savich Theorem.
- (j) What are the various phases in the design of a typical compiler?

UNIT – I

- Q2 (a) Show that the set $L=\{a^p/\text{where } p \text{ is prime}\}$ is not regular. (5)
- (b) Design a DFA to accept the following language :- (5)
- $L=\{w/w \in \{0,1\}^* \text{ and } w \text{ when interpreted as a number is not divisible by } 3.\}$

OR

Q3 (a) Convert the following NFA to a DFA :-

(5)

	0	1
$\rightarrow p$	p,q	P
q	r	r
r	s	\emptyset
s	s	s

(b) Convert the following Mealy machine into Moore machine :- (5)

Present State	Next state			
	Input a=0		Input a=1	
	State	Input	State	Input
→q1	q3	0	q2	0
q2	q1	1	q4	0
q3	q2	1	q1	1
q4	q4	1	q3	0

UNIT II

- Q4 (a) State and prove pumping lemma for CFG. (7)
 (b) Define instantaneous description of a PDA. (3)

OR

- Q5 (a) Design a PDA that accept EVEN Palindrome over {a,b}. (5)
 (b) Given $G = (\{S,A\}, \{a,b\}, P, S)$ where $P = \{S \rightarrow AsA \mid S \mid SS, A \rightarrow Sba \mid ba\}$, S- start symbol. Find the left most and right most derivation of the string $w = aabbbaaa$. (5)

UNIT III

- Q5 (a) Design a Turing Machine that accept the language
 $L = \{w : n_a(w) = n_b(w), w \in \{a,b\}^*\}$.
 (b) Write short note on Church-Turing Thesis.

OR

- Q6 (a) Prove that Halting Problem of Turing Machine is Undecidable. (5)
 (b) Explain reducibility. (5)

UNIT IV

- Q8 Write short notes on the following :- (5+5)
 (a) The P and NP complexity classes.
 (b) Probabilistic computation.

OR

- Q9 (a) Does PCP with two lists $x=(b,bab^3,ba)$ and $y=(b^3,ba,a)$ have a solution ? (5)
- (c) Explain L and NL complexity. (5)